

# Prediction of Sea Ice Motion with Convolutional Long Short-Term Memory Networks

Zisis I. Petrou, *Member, IEEE*, and Yingli Tian\*, *Fellow, IEEE*

**Abstract**—Prediction of sea ice motion is important for safeguarding human activities in polar regions, such as ship navigation, fisheries, and oil and gas exploration, as well as for climate and ocean-atmosphere interaction models. Numerical prediction models used for sea ice motion prediction often require a large number of data from diverse sources with varying uncertainties. In this study, a deep learning approach is proposed to predict sea ice motion for several days in the future, given only a series of past motion observations. The proposed approach consists of an encoder-decoder network with convolutional Long Short-Term Memory (LSTM) units. Optical flow is calculated from satellite passive microwave and scatterometer daily images covering the entire Arctic and used in the network. The network proves able to learn long-time dependencies within the motion time series, whereas its convolutional structure effectively captures spatial correlations among neighboring motion vectors. The approach is unsupervised and end-to-end trainable, requiring no manual annotation. Experiments demonstrate that the proposed approach is effective in predicting sea ice motion of up to 10 days in the future, outperforming previous deep learning networks, and being a promising alternative or complementary approach to resource-demanding numerical prediction methods.

**Index Terms**—Advanced Microwave Scanning Radiometer - Earth Observing System (AMSR-E), Advanced Microwave Scanning Radiometer 2 (AMSR2), Advanced Scatterometer (ASCAT), Arctic sea ice, convLSTM, deep neural networks, drift prediction, optical flow, recurrent neural networks

## I. INTRODUCTION

SEA ice motion significantly affects the thickness distribution of ice in polar regions, causing leads or ridging. It has a critical role in the advection of sea ice out of the Arctic region, whereas it overall influences the ice mass balance and fluxes between the ocean and the atmosphere [1]–[4]. It has been used for the initialization, assimilation, and validation of climate models simulating sea ice dynamics [5]–[9]. On a local level, sea ice motion affects human activities in the Arctic region. Following the continuous decline of sea ice extent during the last decades and the projections for ice-free periods in the future [10]–[12], the potential for more extensive usage of the region for shipping, fisheries, oil and gas exploration, and tourism has been raised [13]. In order

to safeguard human activities and enhance climate modeling, accurate short-term predictions of sea ice motion for several days in the future are increasingly important.

Predictions of sea ice motion, together with sea ice extent and related variables, have almost exclusively been attempted using numerical prediction models, including fully coupled atmosphere-ocean global climate models, statistical regression-based approaches, and heuristic methods [14]–[19]. A number of models have been designed to address seasonal, interannual, and decadal predictions [13], [20], whereas others focus on short-term forecasting [21], with the latter being crucial for safe maritime operations. To generate the desired outputs, these models usually rely on a large number of sources of information, including surface winds, ice thickness, water currents, ice collision rheology data, or previous predictions. For a specific time frame or area of interest, the data sources can be limited [22], thus, reducing the applicability of the models. In addition, the model predictions are associated with several sources of uncertainty, including model initial conditions and uncertainties in the input data, e.g., ice thickness data [23], [24].

More specifically, one of the main drivers of sea ice motion, especially in central Arctic, rather than the coastlines, is wind [25], [26]. This is why weather prediction models have been extensively used to predict sea ice motion. Thus, wind prediction limitations of these models consequently limit the accuracy of sea ice motion prediction. In addition, given that the average sea ice drift speed has increased during the last decades to a much larger degree than wind speed [25], [27], such predictions become more challenging. Additional factors that affect sea ice motion are ocean currents, forcing due to the Coriolis force and density-driven gravitational forcing, and ice cover and internal ice strength, with the latter ones acting as resisting motion factors.

In this study, we propose a short-term prediction approach based on single-source data time series. In particular, we employ sea ice motion data calculated from sequences of daily passive microwave and scatterometer satellite images and predict motion for several days in the future. Our proposed approach is based on deep neural networks, specifically convolutional Long Short-Term Memory (LSTM) networks [28], and offers several advantages compared with the aforementioned numerical model prediction paradigm: i) it relies on a single source of data, thus, it is prone to single-source uncertainties; ii) the data are available on a daily basis and cover the entire Arctic; iii) the proposed approach is completely unsupervised and automated, i.e., the proposed network is trained end-to-end without requiring any human annotation of the data; and iv)

Manuscript received Aug. 6, 2018. Revised Dec. 9, 2018 and Feb. 24, 2019. Accepted Mar. 21, 2019. This work was supported in part by ONR grant N000141310450 and NSF grant IIS-1400802.

Z. I. Petrou is with the Department of Electrical Engineering, The City College, The City University of New York, New York, NY, 10031 USA. e-mail: zpetrou@ccny.cuny.edu.

Y. Tian is with the Department of Electrical Engineering, The City College and the Department of Computer Science, The Graduate Center, The City University of New York, New York, NY, 10031 USA. e-mail: ytian@ccny.cuny.edu.

\*Corresponding author.

while the methodology explicitly ignores the aforementioned factors that affect sea ice motion prediction (wind, ocean currents, sea ice cover), these factors can be implicitly modeled through the calculations of spatial and temporal correlations of sea ice motion. In addition, contrary to the only previous deep learning approach for sea ice motion prediction [29], our proposed convolutional LSTM approach can explicitly capture spatial relationships among neighboring motion vectors.

Our study is organized as follows: Section II discusses previous work on motion prediction. Section III presents the data used in the study and Section IV details our proposed method. Experimental results are drawn and discussed in Section V. Conclusions are given in Section VI.

## II. RELATED WORK

Recurrent neural networks (RNN) have been used in a variety of remote sensing applications, including image classification [30], [31], automatic clustering of multispectral images [32]; spatiotemporal prediction of snow depth and distribution driven by meteorological data [33]; retrieval of areal extent of snow cover [34]; rainfall nowcasting from multi-satellite passive-sensor images [35]; and estimation of soil moisture dynamics [36]. In particular, LSTM networks have been additionally employed in image classification [37]; image captioning [38]; land cover change detection [39]; semantic understanding of high resolution images [40]; and supervised texture segmentation [41]. Contrary to the aforementioned applications, LSTM networks are employed in this study to encode spatiotemporal information, more specifically sea ice motion, from 2D time-series and predict future time-series in the 2D space for several days in the future.

Prediction of motion has been an increasingly studied field. A number of approaches have focused in predicting motion trajectories of image pixels or objects in the 2D space [42]–[44]. Despite the similarities, the objective of this study is different, as we do not aim at predicting the trajectory of specific sea ice floes, but instead at predicting the motion in the dense image field, i.e., for every pixel, for several time instances. Prediction of traffic or crowd flow is another relevant field to our study where deep learning techniques have been proposed recently [45]–[49]. Ma *et al.* [46] proposed a 2D image representation of spatiotemporal traffic and a convolutional neural network (CNN) approach for short-term traffic prediction. Similar to [49], space is considered as one dimension, with spatial correlations captured in 1D space, and thus, different from the 2D desired motion in this study. Closer to the problem formulation in this study, Yu *et al.* [45] used CNN to generate 2D spatial traffic features and fully connected LSTM for prediction. Zhang *et al.* [47], [48] leveraged the existence of motion temporal patterns and proposed the fusion of temporal closeness, period, and seasonal trend to capture temporal dependencies for short-term crowd flow prediction. The method could be promising for sea ice motion prediction under the assumption of seasonality patterns of the motion, which have not been observed on our available single-year data. Furthermore, several approaches have employed static images to predict future image frames [50]–[52]. Such approaches are not appropriate in our study, since single-time

images, or even single-time sea ice motion, convey limited information on future sea ice motion and any prediction would be mostly arbitrary.

A number of approaches based on image time series as input for future prediction have been proposed recently, mainly in the field of unsupervised video prediction [28], [29], [53]–[61]. Srivastava *et al.* [59] proposed an encoder-decoder architecture based on LSTM to predict a number of future images from an input sequence of images. A variation of the network using a predicted frame as additional input for the next prediction provided the best results. Shi *et al.* [28] introduced the idea of convolutional LSTM (convLSTM) networks, that besides the ability to encode and decode temporal information, were able to capture spatial relationships between neighboring pixels for precipitation nowcasting. The idea of convolutional LSTM models has further been employed in prediction studies [53], [55], [56], [58]. A recent study used optical flow, i.e., dense 2D sea ice motion, directly as input to an encoder-decoder LSTM network to predict sea ice motion for several days in the future [29]. However, the input in this approach was converted to a 1D vector to be handled by the fully connected LSTM networks, thus ignoring spatial relationships between neighboring pixels.

In this study we propose a deep convolutional LSTM approach for sea ice motion prediction. A major difference with aforementioned frame prediction approaches is that we do not try to predict future images and use these images to estimate motion. Instead, we use optical flow time series as input to the convolutional LSTM network and directly predict motion for several days in the future. Contrary to [29], the proposed convolutional structure is able to capture spatial relationships among neighboring pixels, whose motion is highly correlated.

## III. DATA

The principal data used to train the prediction model are a large number of Level-3 brightness temperature images from the Advanced Microwave Scanning Radiometer - Earth Observing System (AMSR-E) sensor on NASA's Aqua satellite [62]. The spatial resolution of the images is 12.5 km. In total, a number of 276 daily images, from January 1st to October 3rd, 2011, are collected, most of them used for the model training. The images are of horizontal polarization at 36.5 GHz and cover the entire Arctic (Fig. 1), with the coordinates of their corners being: top-left 30.98°N, 168.35°E; bottom-left 33.92°N, 80.74°W; top-right 31.37°N, 102.34°E; bottom-right 34.35°N, 9.97°W.

A variety of data is used to evaluate the prediction model, coming from different sensors, properties, and periods of the year. First, a random sample from the aforementioned AMSR-E images is used for testing. In addition, images from the Advanced Microwave Scanning Radiometer 2 (AMSR2) onboard the Global Change Observation Mission - Water (GCOM-W) satellite are used. AMSR2 data from both 36 GHz and 89 GHz bands are collected from the winter (Feb. 21 – Mar. 24, 2018) and summer (Aug. 21 – Sep. 30, 2018) seasons [63]. In particular, Level-3 horizontal polarization brightness

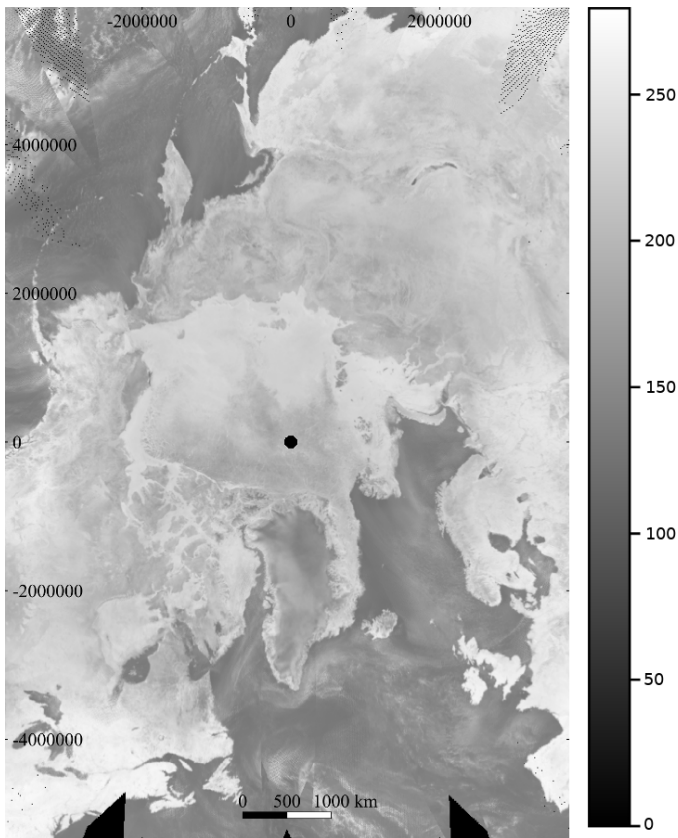


Fig. 1. AMSR-E image from January 1, 2011, with brightness temperature colorbar (in K). The image is projected on the North Polar Stereographic projection [65].

temperature images of 10 km spatial resolution are collected. The images are downsampled to 12.5 km resolution to have the same extent and size to the AMSR-E images. In order to evaluate the performance of the approach beyond passive microwave data, images from the Advanced Scatterometer (ASCAT) onboard the EUMETSAT METOP satellite are also collected for testing, both from the winter (Feb. 19 – Mar. 30, 2017) and the summer (Aug. 28 – Sep. 27, 2017) seasons [64]. In particular, daily multi-orbit incidence angle normalized sigma-0 (sigma-0 at 40 degree incidence angle) Arctic images processed by the multi-variate Scatterometer Image Reconstruction algorithm with filtering (SIRF) are used. The images are downsampled from 4.45 km to 11.20 km, so their width matches the width of the AMSR-E and AMSR2 images.

All images are projected in the National Snow and Ice Data Center (NSIDC) Polar Stereographic North grid, with 70°N latitude of true scale and the origin longitude at 45°E [65]. The images are scaled between the overall minimum and maximum values of the entire set and converted to 8-bit images for memory and processing efficiency. The open water and land is masked out from each image, based on daily masks generated by or distributed with the above products.

As a note, a main reason for the selection of the data sources above for this study, besides the previous successful use in sea ice motion estimation studies and the wide spatial coverage, is the availability of daily data. This temporal

resolution is necessary to allow daily predictions. Thus, such large swath width radiometer and scatterometer data are more appropriate for the requirements of this study than smaller swath width data sources, such as Synthetic Aperture Data (SAR). Although SAR has proven accurate in providing high resolution sea ice motion estimation, the daily availability of images covering the entire Arctic is currently limited [66].

Note that the images and their corresponding sea-ice masks used in the experiments in this manuscript, for the AMSR-E, AMSR2, and ASCAT sensors are available at DOI: 10.21227/f87y-by42 with the title of "Data for Prediction of Sea Ice Motion with Convolutional Long Short-Term Memory Networks."

## IV. METHODS

### A. Optical flow estimation

Optical flow is calculated for each pair of masked images of consecutive days for AMSR-E, AMSR2, and ASCAT data, respectively. Given a pair of images, the output of the calculation is a 3D tensor with the two axes representing the axes of the original 2D images in pixels, and the third axis including the latitudinal and longitudinal motion of sea ice for each pixel from the first to the second image. As a note, the terms "latitudinal" and "longitudinal" motion are used in the paper to indicate motions in the vertical and horizontal axis of the reprojected images, respectively. Despite the fact that, due to the selected map projection, the terms do not align with the geographic latitude and longitude coordinates (e.g., positive longitudinal motion in the upper part of the projected image describes motion toward decreasing geographic longitudes), the terms are selected to highlight the georeferenced nature of the analyzed motion. The optical flow method proposed in [67] is adopted, proven more accurate than traditionally employed pattern matching in sea ice motion estimation and able to provide dense calculation in the continuous (sub-pixel) space [66].

The calculated optical flow data are grouped in overlapping sequences including  $T + P$  consecutive-day flow instances, where the first  $T$  flow instances represent the input to the prediction model and the last  $P$  ones the desired output.

### B. Conditioned convolution LSTM network

1) *Convolutional LSTM unit*: The proposed network consists of connected convolutional LSTM units, which have the typical structure of LSTM with peephole connections [28]. The structure of an LSTM unit is drawn in Fig. 2.

Each LSTM unit consists of a *memory cell*  $C$ , which is connected with an *input*,  $i$ , *forget*,  $f$ , and *output*,  $o$ , logistic sigmoidal gates. This structure allows the memory cell to sum activities over time and capture long-term properties, counteracting exploding and vanishing gradient problems that limit vanilla RNN networks. At time  $t$ , the unit gets as input the  $t$ -th optical flow of a sequence,  $X_t$ , and the output, or *hidden state*, from the previous step,  $H_{t-1}$ . In the case of the encoder,  $X_t$  comes from the input optical flow sequence, whereas in the case of the decoder from the predicted sequence. The two input sources,  $X_t$  and  $H_{t-1}$ , pass through the input and forget

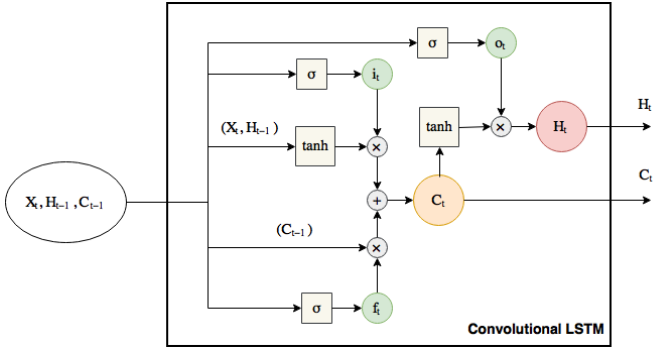


Fig. 2. Representation of a LSTM unit. The inputs of the unit at time  $t$  are shown in the ellipse outside the box. Arrows with input variables in parenthesis denote that only the specific input(s) is(are) passed. The outputs of the LSTM unit are the updated cell,  $C_t$ , and hidden,  $H_t$ , states.

gates and update the cell state. The updated cell state,  $C_t$ , pass together with  $X_t$  and  $H_{t-1}$  through the output gate and update the hidden state of the unit through a tanh non-linearity. All  $H_t$ ,  $i_t$ ,  $f_t$ , and  $o_t$  are 3D arrays whose last two dimensions match the width and height dimensions of  $X_t$ . The following formulas describe the overall LSTM connections:

$$\begin{aligned} i_t &= \sigma(W_{xi} * X_t + W_{hi} * H_{t-1} + W_{ci} \odot C_{t-1} + b_i), \\ f_t &= \sigma(W_{xf} * X_t + W_{hf} * H_{t-1} + W_{cf} \odot C_{t-1} + b_f), \\ C_t &= f_t \odot C_{t-1} + i_t \tanh(W_{xc} * X_t + W_{hc} * H_{t-1} + b_c), \\ o_t &= \sigma(W_{xo} * X_t + W_{ho} * H_{t-1} + W_{co} \odot C_{t-1} + b_o), \\ H_t &= o_t \odot \tanh(C_t), \end{aligned}$$

where  $\sigma$  represents the sigmoid function,  $W$  the weight matrices, and  $b$  the biases. The peephole connection weight matrices  $W_{ci}$ ,  $W_{cf}$ , and  $W_{co}$  are diagonal, whereas the rest are dense. Convolutions are denoted by  $*$ , whereas  $\odot$  stands for the Hadamard product.

2) *LSTM network*: The proposed prediction network has an encoder-decoder structure with convolutional LSTM units (Fig. 3). For a specific sequence, the input daily flows,  $X$ , are given sequentially as input to the LSTM encoder and transformed into a compact representation. The encoded representation is then fed to the decoder network that predicts the next daily optical flows. The output is fed to a forward convolutional layer that reconstructs it to the same feature dimensions as the input. During the training of the network, the predicted flows,  $\hat{Y}_t$ ,  $j = T + 1, \dots, T + P$ , are compared with the corresponding calculated flows for the same days,  $X_t$ ,  $t = T + 1, \dots, T + P$ . Thus, the entire network is end-to-end trainable in an unsupervised fashion requiring no manual annotation.

Fig. 4 draws in more detail the interactions among the network components. As depicted, the last states and cell outputs of the encoder are copied to the decoder network. The encoder and decoder can consist of multiple layers of LSTM units stacked together, with the output,  $H$ , of one layer being the input of the next one. Contrary to the original convolutional LSTM model [28], our decoder network is conditioned on the previous output [59]. This structure allows the decoder

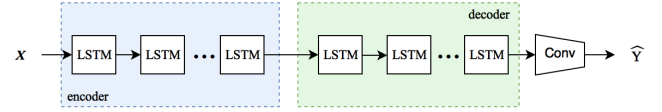


Fig. 3. Overview of the structure of the proposed convolutional LSTM prediction network.  $X$  represents the optical flow input sequence, ‘LSTM’ and ‘Conv’ stand for convolutional LSTM and forward convolutional layers, respectively, and  $\hat{Y}$  represents the predicted flow array.

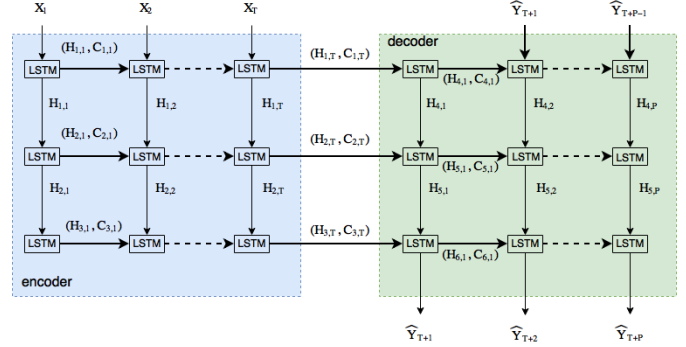


Fig. 4. Breakdown of the encoder-decoder structure of the proposed prediction network.  $X_i$  represents the  $i$ -th optical flow array of the input sequence  $X$ ,  $\hat{Y}_j$  represents the  $j$ -th predicted flow array;  $C_{l,t}$  and  $H_{l,t}$  stand for the cell and hidden state of a convolutional LSTM unit in layer  $l$  and time  $t$ .

network to use as additional input for each predicted flow,  $\hat{Y}_t$ ,  $t = T + 1, \dots, T + P$ , the previous prediction,  $\hat{Y}_{t-1}$ , with the exception of the first prediction,  $\hat{Y}_{T+1}$ , where the encoded information is the only input to the decoder (Fig. 4). During training, the observed optical flow in time  $t - 1$  is used as input, whereas during validation and testing the predicted flow is used instead. This modification is supported by the notion that sea ice motion between consecutive days usually does not change dramatically as far as magnitude and direction are concerned, at least at the 12.5 km spatial and the daily temporal scale of the imagery. There can be regular direction and speed changes on sub-kilometer and sub-daily scales, due to tides, inertial effects, and ice leads and ridging [68], [69], but their effects are averaged out on the scales of analysis of this study. Thus, prior knowledge of the predicted motion at time  $t - 1$  is expected to constrain and enhance the prediction at time  $t$ . Furthermore, in [28] the outputs from all decoder LSTM layers are concatenated and fed to the  $1 \times 1$  convolutional layer to produce the final prediction. On the contrary, in our network only the output of the last LSTM layer is fed to the final  $1 \times 1$  convolutional layer. The notion of this simpler connection network is to keep the role of each layer distinct in the propagation of information between layers, so network optimization is more focused and targeted during training. In addition, the number of network parameters is also decreased in this final layer, preventing overfitting.

3) *Optimization and loss*: Backpropagation through time (BPTT) and Root Mean Square Propagation (RMSProp) [70] are used for minibatch training of our network. During training, having an optical flow sequence  $\{X_1, \dots, X_T\}$  as input,

the predicted sequence  $\{\hat{Y}_{T+1}, \dots, \hat{Y}_{T+P}\}$  is compared with the actual sequence  $\{Y_{T+1}, \dots, Y_{T+P}\}$ . Instead of the commonly used squared loss [28], [29], [59], we additionally employ  $l_2$  gradient difference loss [57], to penalize changes in differences between neighboring pixels beyond the expected ones. Our final loss function is

$$\begin{aligned}
 L(\hat{Y}, Y) = & a \sum_{i,j,k} |Y_{i,j,k} - \hat{Y}_{i,j,k}|^2 \\
 & + b \sum_{i,j,k} \left| |Y_{i,j,k} - Y_{i-1,j,k}| - |\hat{Y}_{i,j,k} - \hat{Y}_{i-1,j,k}| \right|^2 \\
 & + b \sum_{i,j,k} \left| |Y_{i,j,k} - Y_{i,j-1,k}| - |\hat{Y}_{i,j,k} - \hat{Y}_{i,j-1,k}| \right|^2,
 \end{aligned} \tag{1}$$

where  $i$ ,  $j$ , and  $k$  are width, height, and depth, pixel indices, respectively. The first summation term represents the squared loss, whereas the last two terms the gradient loss. The weights  $a \in \mathbb{R}$  and  $b \in \mathbb{R}$  define the relative contribution of the two terms in the overall loss.

## V. RESULTS AND DISCUSSIONS

### A. Experimental settings

The daily optical flow arrays form sequences of 20 consecutive-day arrays. In each sequence, the first 10 arrays are used as input ( $T = 10$ ) and the last 10 as the ground-truth prediction output ( $P = 10$ ). Data from AMSR-E are used to train the prediction model. A number of temporally overlapping sequences are randomly selected to form the validation set during the network training. Another set of temporally overlapping sequences are randomly selected as testing set, under the condition of having no common dates with the validation set. The remaining sequences are used as the training set, with no common dates with the validation and testing sets. The sequences are split in  $32 \times 32$  spatially non-overlapping patches over the longitude and latitude image dimensions, forming sequences of 20 such patches. For training efficiency, the sequences with no sea ice pixels are removed from the training and validation sets. However, since we aim at simulating real-life conditions and make the algorithm agnostic of the underlying surface, we keep training and validation sequences that include non-moving (e.g., land, land-fast ice) pixels together with moving (sea ice) pixels, so that the algorithm can learn zero-motion patterns as well. The testing sets consist of sequences covering the entire Arctic region, including both moving and non-moving regions.

Following the above process, the training and validation sets include 32,087 and 1,208 sequences of 20  $32 \times 32$  optical flow patches from AMSR-E data, respectively. The testing data include i) 5,852 sequences of patches from AMSR-E; ii) 13,718 and 14,440 sequences from ASCAT winter and summer data, respectively; and iii) 20,216 sequences from each of AMSR2 36 GHz and 89 GHz winter data type and 21,280 sequences from each summer data type.

We use a 3-layer encoder and a 3-layer decoder network. The number of hidden states of the convolutional LSTM

TABLE I  
COMPARISON OF THE PREDICTED OPTICAL FLOW WITH THE REFERENCE OPTICAL FLOW VECTORS FOR THE AMSR-E DATA, FOR EACH PREDICTION STEP IN THE FUTURE ('FUT'). COLUMN 'VECTORS' REPORTS THE TOTAL NUMBER OF VECTORS COMPARED. MEAN-ABSOLUTE ERROR (MAE) AND ROOT MEAN-SQUARED ERROR (RMSE) ARE REPORTED FOR THE LATITUDINAL (X) AND LONGITUDINAL (Y) MOTION AXES, BOTH IN KM. THE AVERAGE ERRORS FROM ALL STEPS ARE ALSO REPORTED.

fut	vectors	x-MAE	x-RMSE	y-MAE	y-RMSE
1	807626	<b>2.34</b>	<b>3.25</b>	<b>2.11</b>	<b>3.07</b>
2	803467	2.65	3.69	2.32	3.44
3	799080	2.78	3.84	2.18	3.23
4	794545	3.00	4.10	2.30	3.35
5	790216	3.28	4.46	2.50	3.62
6	786609	3.37	4.60	2.68	3.84
7	782872	3.40	4.62	2.76	3.93
8	779041	3.44	4.63	2.86	4.05
9	774893	3.39	4.56	3.03	4.24
10	770026	3.28	4.40	3.09	4.33
Avg.	788837.5	3.09	4.21	2.58	3.71

layers are 128, 64, and 32, respectively, whereas the state-to-kernel size is  $5 \times 5$ . We use minibatch training of 16 sequences, a learning rate of 0.001 and a decay rate of 0.9 for RMSProp optimization. The size of LSTM layers and the learning and decay rates are in line with related studies [28], [55], [58]; we experiment with varying values without noticing significant changes in performance. The batch size is selected based on experimentation and capabilities of the available GPUs (graphics processing units). As widely employed, the convolutional LSTM layer weights,  $W$ , were initialized from a uniform distribution in  $[-1, 1]$ , whereas the initial biases,  $b$ , were set to zero. We select the  $l_2$  gradient loss function described in eq. (1), which outperformed  $l_2$ ,  $l_1$ , and  $l_1$  gradient loss functions in our experiments. The weights of the loss function in eq. (1),  $a$  and  $b$ , are set to 1.

We compare our conditioned convolutional LSTM network with the fully connected conditioned LSTM network by Petrou and Tian [29] and the convLSTM network by Shi *et al.* [28]. For the former, we employ a 2-layer encoder-autoencoder-decoder architecture with 4096 and 2048 hidden states, uniform initialization of the weight matrices and biases set to 1, based on recommendations in [71]. The two convLSTM versions have the same parameters as our network, one with the originally proposed  $3 \times 3$  state-to-kernel size and one with  $5 \times 5$ . Based on the performance in the validation set, the same number of 50 epochs is selected to train all networks.

### B. Comparison with reference optical flow

The predicted optical flow from our proposed network for ten days in the future is compared with the reference optical flow for the same days. Thus, the average difference of the predicted 2D motion vector at each pixel with the reference optical flow at the same pixels is calculated.

1) *AMSR-E data*: Table I shows the mean-absolute error (MAE) and root mean-squared error (RMSE) between the vectors for the latitude ('x') and longitude ('y') axes for 10 prediction steps, as well as the overall average performance.

As expected, the best predictions—highlighted in bold—are made for the first prediction step, i.e., the first day after the

observed optical flow. The performance of the prediction starts degrading as predictions move further into the future. In the y-axis the worst performance is observed at the 10-th prediction step, for the x-axis at the 8-th step, whereas overall the errors are larger the later the predictions are into the future. The MAE errors follow a quasi-linear increase as the predictions move into the future. It is noteworthy that the worst error predictions are less than by 50% worse than the best early predictions. This indicates that prediction holds a similar, not quickly decreasing performance after several prediction steps in the future.

2) *Winter ASCAT and AMSR2 data:* Fig. 5 draws the MAE errors for the ASCAT and AMSR2 data during the dry winter season for the 10 prediction steps. Masking out non-sea ice pixels, about 1.5 million and 1.1 million motion vectors are included per prediction step. The predictions with ASCAT data follow more closely the observed optical flow vectors than the predictions from AMSR2 data for all prediction steps, as far as the combined x- and y-axis errors are concerned. The predictions from 36GHz AMSR2 data are consistently better than the 89 GHz AMSR2 data, but following a highly correlated pattern per prediction step. For all sources of data, the predictions get less accurate as they move further in the future. However, similar to the ASMR-E data, the prediction drop from the first to the tenth prediction step is only about 20% or lower for any of the ASCAT and AMSR2 data, demonstrating that the performance of the model remains stable after several days in the future. It is also noteworthy that predictions, mostly from the ASCAT data, have similar accuracy with the predictions from AMSR-E data reported in Table I. This demonstrates that our model is transferable to data sources different than the ones used to train it, and highlights the importance of using optical flow data rather than sensor-specific raw image values, such as brightness temperature.

3) *Summer ASCAT and AMSR2 data:* The MAE errors for the ASCAT and AMSR2 data during the melt summer season are drawn in Fig. 6 for the 10 prediction steps. After masking out non-sea ice pixels, each prediction step considers about 320,000 and 565,000 vectors from ASCAT and AMSR2 data, respectively. As in the dry season, the predictions with ASCAT data are consistently more accurate than AMSR2 data. For most prediction steps, the predictions with 36GHz AMSR2 data are not significantly worse than with ASCAT data. On the contrary, 89 GHz AMSR2 errors are almost double as high as 36 GHz AMSR2 for most prediction steps. As reported in previous studies [72], [73], 89 GHz microwave data are more affected by atmospheric and surface properties than 36 GHz and lead to less accurate estimation of sea ice motion. Such atmospheric conditions, more intense during the summer melt season, have affected the accuracy of the calculated optical flow, used as input and reference data. Thus, the input data from 89 GHz can include inconsistent and erroneous motion patterns that the model has not been trained to identify, and thus, lead to predictions less consistent with the calculated reference flow.

4) *Marginal ice zone and Canadian Archipelago:* Besides regions of thick ice, mainly in the center of Arctic and around

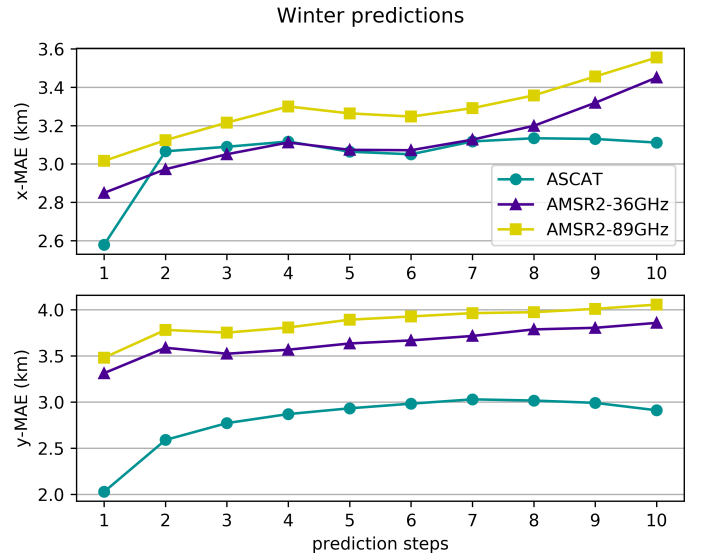


Fig. 5. Comparison of the predicted optical flow with the reference optical flow vectors, for each prediction step in the future. MAE errors of the ASCAT and AMSR2 winter data are reported for the latitudinal (x) and longitudinal (y) motion axes.

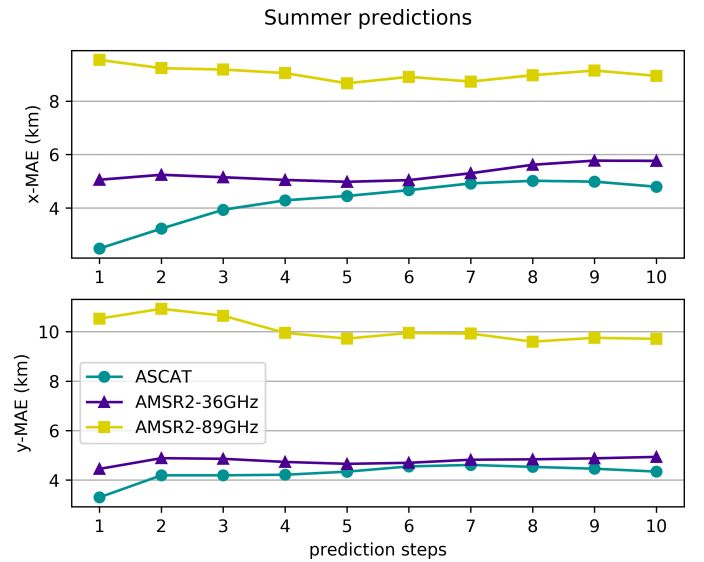


Fig. 6. Comparison of the predicted optical flow with the reference optical flow vectors, for each prediction step in the future. MAE errors of the ASCAT and AMSR2 summer data are reported for the latitudinal (x) and longitudinal (y) motion axes.

the North Pole, the area of study includes several regions of thinner ice, where sea ice motion is usually more intense and may be more challenging to predict. In addition to the evaluation for the entire Arctic presented in the previous sections, we measure the performance of the algorithm separately in two such areas of high operational interest, the Canadian Archipelago and a marginal ice zone east of Greenland (Fig. 7).

Table II reports the MAE errors of the predicted versus the observed reference flow with the ASCAT and AMSR2 data, for both the winter and summer seasons. For space economy, only the first and tenth predictions are reported, in most cases

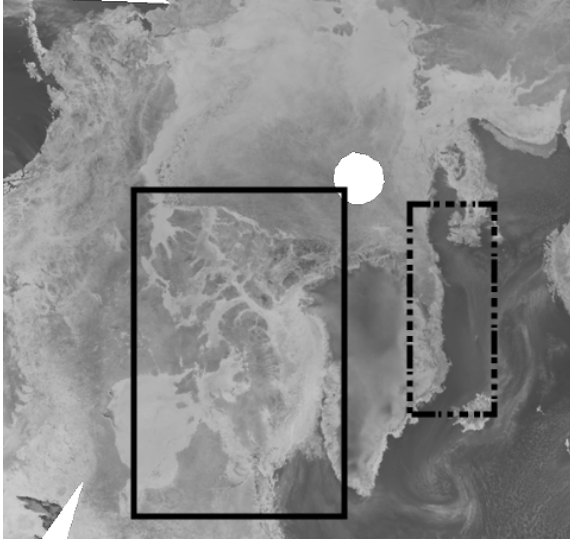


Fig. 7. Canadian Archipelago (solid line) and marginal ice zone (dashed line) regions selected for study, on zoomed view of the 36 GHz AMSR2 image from March 1, 2018.

TABLE II

COMPARISON OF THE PREDICTED OPTICAL FLOW WITH THE REFERENCE OPTICAL FLOW VECTORS, IN THE CANADIAN ARCHIPELAGO FOR ONE AND 10 PREDICTION STEPS IN THE FUTURE ('FUT'). COLUMN 'VECTORS' REPORTS THE AVERAGE NUMBER OF VECTORS COMPARED PER PREDICTION STEP. MEAN-ABSOLUTE ERROR (MAE) IS REPORTED FOR THE LATITUDINAL (X) AND LONGITUDINAL (Y) MOTION AXES. THE AVERAGE ERRORS FROM ALL STEPS ARE ALSO REPORTED. 'W,' AND 'S,' '36,' AND '89' INDICATE WINTER, SUMMER, 36 GHZ, AND 89 GHZ DATA, RESPECTIVELY.

source	vectors	x-MAE (km)		y-MAE (km)	
		fut 1	fut 10	fut 1	fut 10
Canadian Archipelago					
ASCAT-w	327709	1.31	1.89	1.50	2.07
AMSR2-36-w	317075	1.75	2.33	1.83	2.56
AMSR2-89-w	317075	1.88	2.51	1.88	2.96
ASCAT-s	63021	1.21	3.73	1.23	1.80
AMSR2-36-s	187304	4.12	3.99	3.26	3.27
AMSR2-89-s	187304	9.65	7.52	10.46	8.04
Marginal ice zone					
ASCAT-w	68911	2.01	3.16	2.76	4.38
AMSR2-36-w	54819	2.49	4.15	2.64	4.29
AMSR2-89-w	54819	2.60	4.27	2.76	4.18
ASCAT-s	6449	1.91	3.09	2.79	1.30
AMSR2-36-s	29459	5.40	5.70	6.93	7.37
AMSR2-89-s	29459	5.31	5.19	6.20	6.23

representing the lower and upper error limits among the 10 predictions. The errors for the two regions are very similar with the errors reported for the entire Arctic (Fig. 5 and Fig. 6). Our proposed model is able to predict the motion in these challenging regions with similar accuracy as the entire study area. As observed in the previous experiments, the ASCAT data provide more accurate predictions than the AMSR2 data. Similarly, the predictions are more close to the reference data during the dry winter season than the melt summer season.

### C. Comparison with previous methods

We compare our proposed network with previous multi-step prediction approaches, as detailed in Section V-A, on the

TABLE III

COMPARISON OF THE PROPOSED METHOD WITH THE CONDITIONED LSTM APPROACH BY [29] AND THE CONVOLUTIONAL LSTM APPROACH BY [28], THE LATTER WITH  $3 \times 3$  AND  $5 \times 5$  STATE-TO-KERNEL SIZES, ON THE AMSR-E DATA. THE ACCURACY OF COPYING THE LAST INPUT FLOW IS ALSO REPORTED AS 'BASELINE.' THE AVERAGE MAE AND RMSE ERRORS, BOTH IN KM, FOR 10 PREDICTION STEPS ARE SHOWN, FOR THE LATITUDINAL (X) AND LONGITUDINAL (Y) MOTION AXES.

Method	x-MAE	x-RMSE	y-MAE	y-RMSE
baseline	3.61	4.94	3.10	4.43
[29]	3.36	4.53	2.68	<b>3.71</b>
[28] [ $3 \times 3$ ]	3.19	4.35	2.81	4.01
[28] [ $5 \times 5$ ]	3.12	4.24	2.63	3.72
Ours	<b>3.09</b>	<b>4.21</b>	<b>2.58</b>	<b>3.71</b>

AMSR-E data. In addition, the performance of simply copying the last observed input optical flow is considered as baseline. Table III presents the average errors for 10 prediction steps in the future. The conditioned LSTM network by Petrou and Tian [29] performs similarly with the convLSTM network with  $3 \times 3$  state-to-kernel size by Shi *et al.* [28]. Increasing the state-to-kernel size to  $5 \times 5$  captures motion correlations in a larger area and proves beneficial for the performance of the network. Our proposed approach achieves lower errors than both methods, as highlighted in bold. It proves able to capture spatial correlations of motion with the convolutional LSTM layers, whereas conditioning each prediction to the previous one, acts as a priori—unsupervised—knowledge that is beneficial for the next predictions.

### D. Comparison with buoys

Following an unsupervised end-to-end training, our model is trained to minimize the loss against the reference optical flow values. These reference optical flow values, calculated from the corresponding observed AMSR-E image pairs, are considered as a ground-truth during the model training. However, the optical flow calculations with observed data entail errors as evidenced when compared with more accurate validation sources [67]. To get a further estimate on the accuracy of the model predictions, the predicted optical flow vectors are additionally evaluated against buoys from the International Arctic Buoy Programme (IABP) [74]. The buoys have estimated position accuracy around 0.5 km/day [72], [74], providing position accuracy at a much finer scale than the reference optical flow estimated from the coarse 12.5 km resolution AMSR-E images. The daily buoy positions at 12:00 GMT are collected to calculate their motion within consecutive days, and projected to the NSIDC Polar Stereographic North grid [65].

Fig. 8 shows the performance of the proposed approach against the buoy motion, on the AMSR-E data, for every prediction step. The corresponding errors of the reference optical flows are provided too, i.e., the errors calculating the optical flow from observed images on the same days, rather than predicting it. As expected, the reference flow errors remain almost stable as the prediction steps change, since they are independent from the prediction process. On the contrary, the errors of the predictions overall increase as the prediction

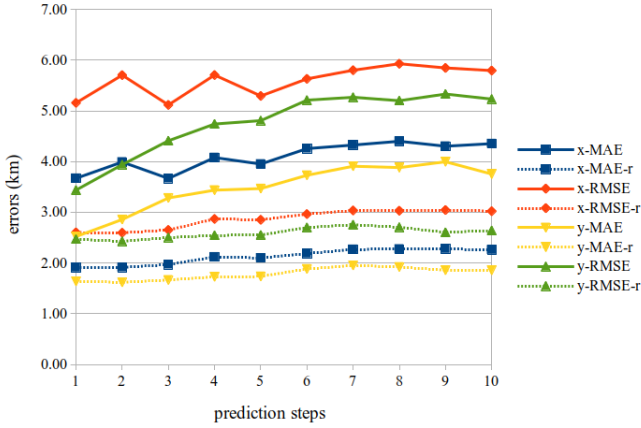


Fig. 8. Comparison of the predicted optical flow and the reference optical flow vectors from the AMSR-E data against buoys, for each prediction step in the future. MAE and RMSE errors are reported for the latitudinal (x) and longitudinal (y) motion axes. The reference data errors are indicated by the prefix ‘-r’.

moves further to the future. Some individual high error values in the first prediction steps on the x axis may be considered as statistical outliers, justified by the fact that the model is not trained to minimize the errors against the buoys, but against the reference flow data.

However, the plots can still offer useful indications on the predictive power of the proposed network. We calculate the relative difference between the corresponding predicted and reference types of error (e.g., the MAE on the x axis for the predicted and reference data), as  $(e_{a,p} - er_{a,p})/e_{a,p}$ , where  $e_{a,p}$  is the average prediction error for axis  $a$ ,  $a = x, y$  and type  $p$ ,  $p = \text{MAE, RMSE}$ , for the 10 prediction steps, and  $er_{a,p,t}$  the corresponding reference error. This relative error lies between 0.84 and 0.95 for the different error measures and axes, indicating that the prediction errors are less than double the reference optical flow error. In addition, it is worth noting that several predicted motions are as accurate as estimations of motion from observed images from previous studies. In particular, pattern matching on similar AMSR-E 36.5 GHz data estimated motion with RMSE error 4.5 km on the x and 4.83 km on the y axis [72]. As observed on Fig. 8, predictions of up to five steps on the y axis have lower error than the motion estimated with observed data from the previous approach. This demonstrates, on the one hand, that the selected optical flow approach offers a solid basis for the training of our network compared with pattern matching approaches, and on the other hand, that our prediction method offers promising results for motion prediction, even without using any buoy information for training. Assimilation of such data in the training process is a candidate future pathway to further increase our method’s prediction accuracy.

Fig. 9 focuses on the sea ice motions within the Arctic Ocean. The predicted motion for one step in the future is drawn, together with the reference optical flow calculated from the corresponding observed AMSR-E images and the buoy motion. Although the optical flow is predicted for each pixel of the image, only 1/14 and 1/9 of the vectors are drawn for

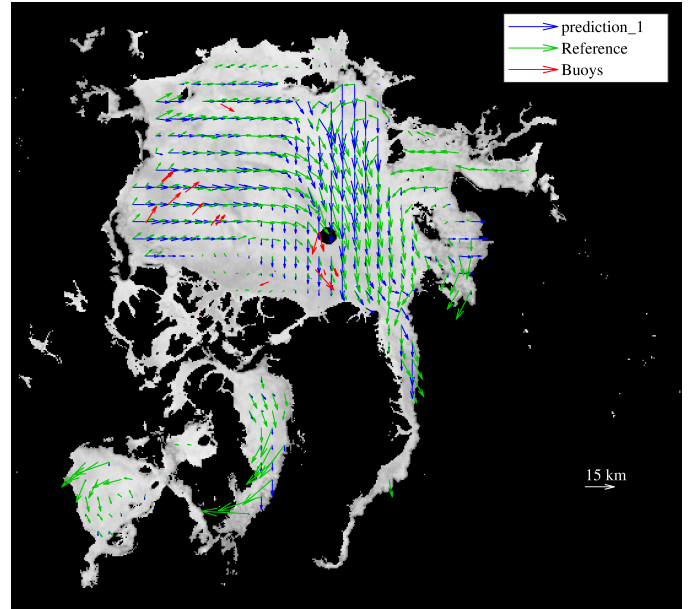


Fig. 9. Focus on predicted sea ice motion for one day in the future with the AMSR-E data, for the dates between May 24 and 25, 2011. The reference optical flow calculated from observed images and buoy motion are also drawn.

clearer illustration for the latitude and longitude axis, respectively. The scale of the motion is also magnified. As observed, the predicted motion follows closely the reference one. For the largest part of the image the predicted and reference motion vectors are highly correlated both in magnitude and direction. It is noteworthy that in certain areas, such as the Beaufort Sea and Chukchi Sea on the left part of the depicted area, the predicted motion does not agree well with the ground truth buoy motion, since no buoy information was used during the network training. Instead, the predictions follow closely the reference flow, which demonstrates the success of our method to extrapolate observations into the future, but also some of its limitations associated with its limited training sources.

### E. Image prediction

We additionally evaluate our network ability to predict future AMSR-E images, given a sequence of past images as input. The depth dimension of the network is changed to 1, since single-band greyscale images are the input and desired output in this case. The rest of the network parameters remain the same. Fig. 10 shows examples of AMSR-E image prediction for one, six, and 10 steps in the future. In particular, a focused view of the predicted image for one step in the future together with the original image are shown in Fig. 10a and Fig. 10c, respectively. The sea ice mask image is also drawn to highlight the areas mostly used during the model training. It is observed that the proposed network is able to predict most of the structure elements of the image, in the sea ice, open ocean, and land areas. Some patch edge effects can be observed in the predicted images, coming from the  $32 \times 32$  pixel predicted patches that were mosaicked to form the final images. In addition, the predicted image appears more blur than the original one, with several sharp details useful



to extract sea ice motion being smoothed out. However, the network proves able to predict the overall structure of the area, even in the parts of no sea ice that were masked out during the training process.

Fig. 10b, Fig. 10d, and Fig. 10f draw the absolute differences between predicted and observed images for one, six, and ten steps in the future, for the dates of May 20, 25, and 29, 2011. The overall predictions for all steps in the future are relatively small, as indicated by the dark pixels in the images. As expected, the first-step predictions are the closest to the observed image. As predictions move further in the future, the differences with the observed images slightly increase. However, most differences appear in areas with non-sea ice pixels, which were masked out during model training. Areas in the central Arctic region, where the main sea-ice layer exists as drawn in Fig. 10e show small differences even for 10-step predictions.

Fig. 11 shows a detail of the predicted image of May 20, 2011, for one day in the future by the proposed convolutional LSTM network and the fully connected network in [29]. The improvement in accuracy and the ability to preserve edges brought by the convolutional LSTM network is observed. Besides these advantages, though, the proposed network appears also more robust to patch effects created by splitting the image (and optical flow) data into sequences of  $32 \times 32$  pixels during the training and prediction processes. These effects clearly affect the quality of the image predicted by the fully connected LSTM network, where the edges around each patch are obvious, creating a tile effect. This effect can hardly be observed in the predicted image by the proposed network. It is noteworthy that the patch sequences are fed to the algorithm during training in a random order, thus spatial relationships among adjacent patches are not explicitly defined. However, the ability of the proposed network to predict images with indistinct patch edges is one more qualitative piece of evidence that the network not only preserves spatial relationships among neighboring pixels, but it provides accurate predictions in absolute terms that allow smooth transitions among adjacent patches.

## VI. CONCLUSION

The convolutional LSTM approach proposed in this study proved able to predict sea ice motion for several days in the future. Optical flow calculated from pairs of AMSR-E images was the only input to the unsupervised end-to-end trainable system requiring no manual annotation. Conditioning each prediction to the previous one, i.e., using as input at each prediction step the previous prediction, took advantage of the temporal correlations that exist in sea ice motion between consecutive days. Besides AMSR-E data, the model was able to provide accurate predictions on data from other sources, AMSR2 and ASCAT, that had not been used for training. Our proposed approach outperformed previous LSTM-based multi-step prediction methods, and although being trained to minimize only reference flow data of sparse resolution, it showed promising results when evaluated against with precision buoy vector data. The approach is, thus, a promising single-source

data-driven alternative or complementary approach to complex numerical methods requiring multi-source data.

## REFERENCES

- [1] S. E. L. Howell, A. S. Komarov, M. Daboor, B. Montpetit, M. Brady, R. K. Scharien, M. S. Mahmud, V. Nandan, T. Geldsetzer, and J. J. Yackel, "Comparing L- and C-band synthetic aperture radar estimates of sea ice motion over different ice regimes," *Remote Sens. Environ.*, vol. 204, pp. 380–391, Jan. 2018.
- [2] W. N. Meier, "Losing Arctic sea ice: observations of the recent decline and the long-term context," in *Sea Ice*, 3rd ed., D. N. Thomas, Ed. Chichester, UK: John Wiley & Sons, 2017, ch. 11, pp. 290–303.
- [3] C. Haas, "Sea ice thickness distribution," in *Sea Ice*, 3rd ed., D. N. Thomas, Ed. Chichester, UK: John Wiley & Sons, 2017, ch. 2, pp. 42–64.
- [4] A. Gettelman and R. B. Rood, *Demystifying Climate Models: A Users Guide to Earth System Models*. Springer Berlin Heidelberg, 2016, ch. 6, pp. 87–108.
- [5] T. Kræmer, H. Johnsen, and C. Brekke, "Emulating Sentinel-1 Doppler radial ice drift measurements using Envisat ASAR data," *IEEE T. Geosci. Remote Sens.*, vol. 53, no. 12, pp. 6407–6418, Dec. 2015.
- [6] A. Berg, L. Axell, and L. E. B. Eriksson, "Comparison between SAR derived sea ice displacement and hindcasts by the operational ocean model HIROMB," in *IEEE Int. Geoscience and Remote Sensing Symp.*, 2013, pp. 3630–3633.
- [7] N. Kimura, A. Nishimura, Y. Tanaka, and H. Yamaguchi, "Influence of winter sea-ice motion on summer ice cover in the Arctic," *Polar Res.*, vol. 32, Nov. 2013, 20193.
- [8] M. L. Van Woert, C. Zou, W. N. Meier, P. D. Hovey, R. H. Preller, and P. G. Posey, "Forecast verification of the Polar Ice Prediction System (PIPS) sea ice concentration fields," *J. Atmos. Ocean. Tech.*, vol. 21, no. 6, pp. 944–957, Jun. 2004.
- [9] W. N. Meier, J. A. Maslanik, and C. W. Fowler, "Error analysis and assimilation of remotely sensed ice motion within an Arctic sea ice model," *J. Geophys. Res.*, vol. 105, pp. 3339–3356, Feb. 2000.
- [10] M. C. Serreze and J. Stroeve, "Arctic sea ice trends, variability and implications for seasonal ice forecasting," *Philos. T. Roy. Soc. A*, vol. 373, 2015, art. no. 20140159.
- [11] J. C. Stroeve, V. Kattsov, A. Barrett, M. Serreze, T. Pavlova, M. Holland, and W. N. Meier, "Trends in arctic sea ice extent from cmip5, cmip3 and observations," *Geophys. Res. Lett.*, vol. 39, no. 16, 2012, art. no. L16502.
- [12] M. Wang and J. E. Overland, "A sea ice free summer arctic within 30 years: An update from cmip5 models," *Geophys. Res. Lett.*, vol. 39, no. 18, 2012, art. no. L18501.
- [13] E. Hawkins, S. Tietsche, J. J. Day, N. Melia, K. Haines, and S. Keeley, "Aspects of designing and evaluating seasonal-to-interannual Arctic sea-ice prediction systems," *Q. J. Roy. Meteor. Soc.*, vol. 142, no. 695, pp. 672–683, 2016.
- [14] A. Dirkson, W. J. Merryfield, and A. Monahan, "Impacts of sea ice thickness initialization on seasonal Arctic Sea ice predictions," *J. Climate*, vol. 30, no. 3, pp. 1001–1017, 2017.
- [15] G. C. Smith, F. Roy, M. Reszka, D. Surcel Colan, Z. He, D. Deacu, J. Belanger, S. Skachko, Y. Liu, F. Dupont, J. Lemieux, C. Beaudoin, B. Tranchant, M. Drévilion, G. Garric, C. Testut, J. Lellouche, P. Pellerin, H. Ritchie, Y. Lu, F. Davidson, M. Buehner, A. Caya, and M. Lajoie, "Sea ice forecast verification in the Canadian Global Ice Ocean Prediction System," *Q. J. Roy. Meteor. Soc.*, vol. 142, no. 695, pp. 659–671, 2016.
- [16] J. Lemieux, C. Beaudoin, F. Dupont, F. Roy, G. C. Smith, A. Shlyaeva, M. Buehner, A. Caya, J. Chen, T. Carrieres, L. Pogson, P. DeRepentigny, A. Plante, P. Pestieau, P. Pellerin, H. Ritchie, G. Garric, and N. Ferry, "The Regional Ice Prediction System (RIPS): Verification of forecast sea ice concentration," *Q. J. Roy. Meteor. Soc.*, vol. 142, no. 695, pp. 632–643, Jan. 2016.
- [17] A. J. Schweiger and J. Zhang, "Accuracy of short-term sea ice drift forecasts using a coupled ice-ocean model," *J. Geophys. Res. Ocean.*, vol. 120, no. 12, pp. 7827–7841, Dec. 2015.
- [18] P. Sakov, F. Counillon, L. Bertino, K. A. Lisæter, P. R. Oke, and A. Korabely, "TOPAZ4: an ocean-sea ice data assimilation system for the North Atlantic and Arctic," *Ocean Sci.*, vol. 8, no. 4, pp. 633–656, Aug. 2012.
- [19] R. H. Preller, P. G. Posey, W. Maslowski, D. Stark, and T. T. C. Pham, "Navy sea ice prediction systems," *Oceanogr.*, vol. 15, no. 1, pp. 44–56, 2002.

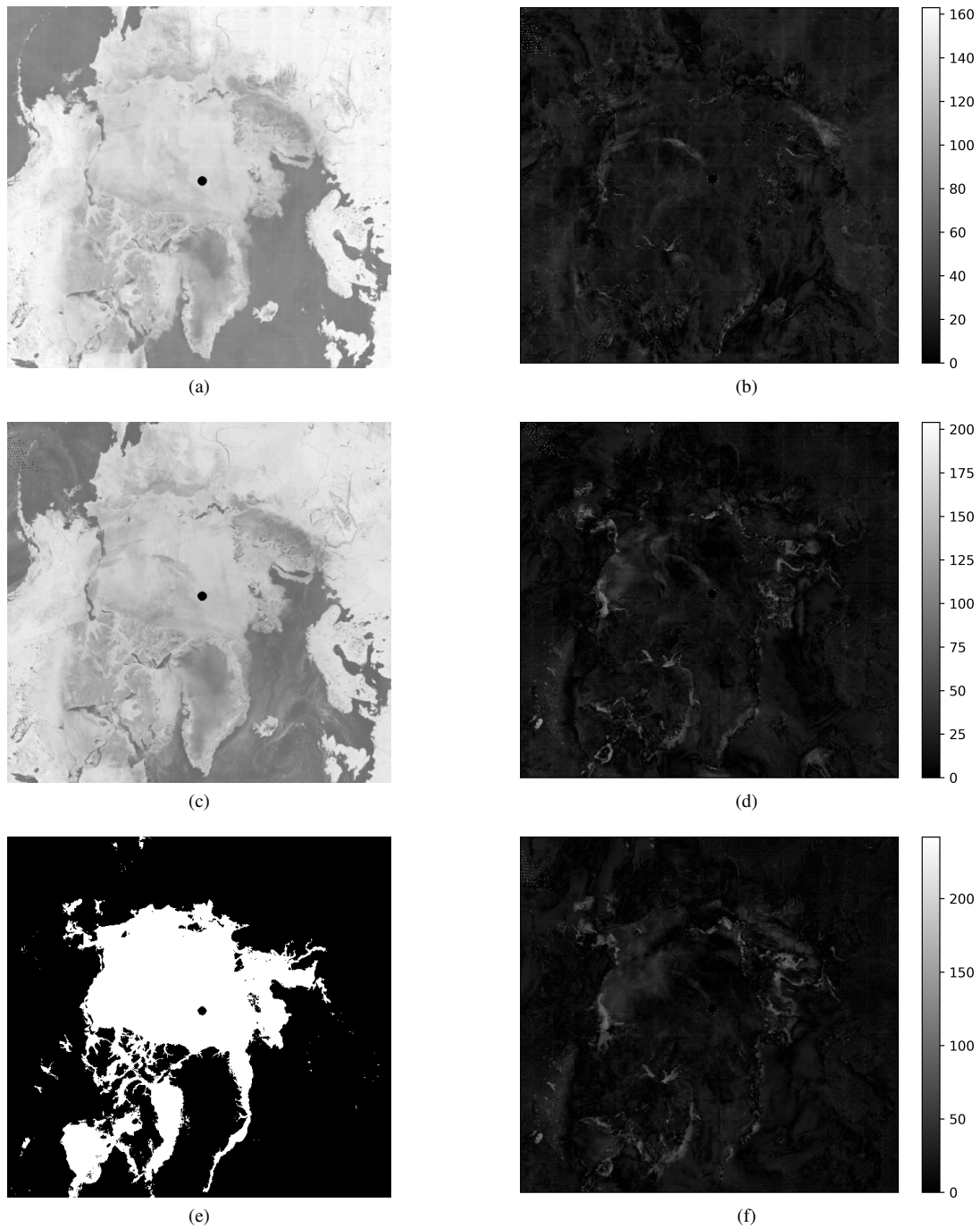


Fig. 10. Focus on (a) the predicted AMSR-E image for one step in the future and (b) the original one from May 20, 2011, together with the corresponding sea ice mask (e). Images on the right show the absolute difference between the original and predicted AMSR-E images for (b) one, (d) six, and (f) 10 days in the future, for the dates May 20, 25, and 29, 2011, respectively.

- [20] V. Guemas, E. Blanchard-Wrigglesworth, M. Chevallier, J. J. Day, M. Déqué, F. J. Doblas-Reyes, N. S. Fučkar, A. Germe, E. Hawkins, S. Keeley, T. Koenigk, D. Salas y Méliá, and S. Tietsche, "A review on Arctic sea-ice predictability and prediction on seasonal to decadal time-scales," *Q. J. Roy. Meteor. Soc.*, vol. 142, no. 695, pp. 546–561, 2016.
- [21] D. A. Hebert, R. A. Allard, E. J. Metzger, P. G. Posey, R. H. Preller, A. J. Wallcraft, M. W. Phelps, and O. M. Smedstad, "Short-term sea ice forecasting: An assessment of ice concentration and ice drift forecasts using the U.S. Navy's Arctic Cap Nowcast/Forecast System," *J. Geophys. Res. Ocean.*, vol. 120, no. 12, pp. 8327–8345, Dec. 2015.
- [22] F. Kauker, T. Kaminski, R. Ricker, L. Toudal-Pedersen, G. Dybkjaer, C. Melsheimer, S. Eastwood, H. Sumata, M. Karcher, and R. Gerdes, "Seasonal sea ice predictions for the Arctic based on assimilation of remotely sensed observations," *Cryosph. Discuss.*, vol. 9, pp. 5521–5554, Oct. 2015.
- [23] L. W. A. De Silva, H. Yamaguchi, and J. Ono, "Ice–ocean coupled computations for sea-ice prediction to support ice navigation in Arctic sea routes," *Polar Res.*, vol. 34, Nov. 2015, art. no. 25008.
- [24] R. Msadek, G. A. Vecchi, M. Winton, and R. G. Gudgel, "Importance of initial conditions in seasonal predictions of Arctic sea ice extent," *Geophys. Res. Lett.*, vol. 41, no. 14, pp. 5208–5215, 2014.
- [25] G. Spreen, R. Kwok, and D. Menemenlis, "Trends in arctic sea ice drift and role of wind forcing: 1992–2009," *Geophys. Res. Lett.*, vol. 38,

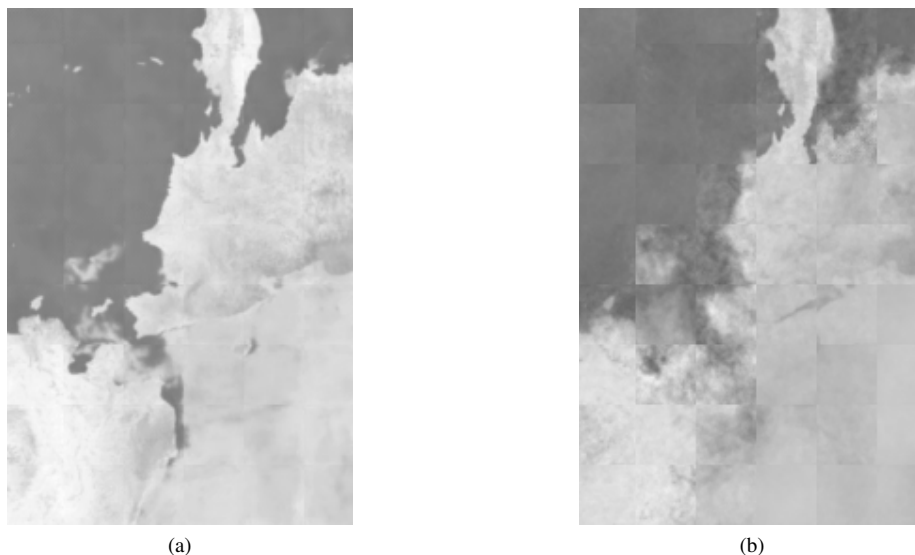


Fig. 11. Detail of predicted AMSR-E image by the proposed convolutional LSTM network (left) and the fully connected LSTM network by [29] (right) for one day in the future. The depicted detail is from the upper-left part of the original image, including the Chukchi Sea and the Bering Strait, from May 20, 2011.

- no. 19, Oct. 2011, 119501.
- [26] M. Steele, J. Zhang, D. Rothrock, and H. Stern, "The force balance of sea ice in a numerical model of the Arctic Ocean," *J. Geophys. Res. Oceans*, vol. 102, no. C9, pp. 21 061–21 079, Sep. 1997.
- [27] P. Rampal, J. Weiss, and D. Marsan, "Positive trend in the mean speed and deformation rate of Arctic sea ice, 1979–2007," *J. Geophys. Res.*, vol. 114, no. C5, May 2009, art. no. C05013.
- [28] X. Shi, Z. Chen, H. Wang, D.-Y. Yeung, W. Wong, and W. Woo, "Convolutional LSTM network: A machine learning approach for precipitation nowcasting," in *Advances in Neural Information Processing Systems* 28, 2015, pp. 802–810.
- [29] Z. I. Petrou and Y. Tian, "Prediction of sea ice motion with recurrent neural networks," in *IEEE Int. Geoscience and Remote Sensing Symp.*, Fort Worth, TX, 2017, pp. 5422–5425.
- [30] L. Mou, P. Ghamisi, and X. X. Zhu, "Deep recurrent neural networks for hyperspectral image classification," *IEEE T. Geosci. Remote Sens.*, vol. 55, no. 7, pp. 3639–3655, Jul. 2017.
- [31] E. Maggiori, G. Charpiat, Y. Tarabalka, and P. Alliez, "Recurrent neural networks to correct satellite image classification Maps," *IEEE T. Geosci. Remote Sens.*, vol. 55, no. 9, pp. 4962–4971, Sep. 2017.
- [32] P. Koprinkova-Hristova, K. Alexiev, D. Borisova, G. Jeleu, and V. Atanassov, "Recurrent neural networks for automatic clustering of multispectral satellite images," in *Image and Signal Processing for Remote Sensing XIX, Proc. SPIE*, L. Bruzzone, Ed., vol. 8892, Dresden, Germany, 2013, pp. 88 920X–1–88 920X–8.
- [33] T. Sauter, B. Weitzenkamp, and C. Schneider, "Spatio-temporal prediction of snow cover in the Black Forest mountain range using remote sensing and a recurrent neural network," *Int. J. Climatol.*, vol. 30, no. 15, pp. 2330–2341, Dec. 2010.
- [34] J. J. Simpson and T. J. McIntire, "A recurrent neural network classifier for improved retrievals of areal extent of snow cover," *IEEE T. Geosci. Remote Sens.*, vol. 39, no. 10, pp. 2135–2147, Oct. 2001.
- [35] F. S. Marzano, G. Rivolta, E. Coppola, B. Tornassetti, and M. Verdecchia, "Rainfall nowcasting from multisatellite passive-sensor images using a recurrent neural network," *IEEE T. Geosci. Remote Sens.*, vol. 45, no. 11, pp. 3800–3812, Nov. 2007.
- [36] Y. C. Tzeng, K. T. Fan, C. Y. Lin, Y. J. Lee, and K. S. Chen, "Estimation of soil moisture dynamics using a recurrent dynamic learning neural network," in *IEEE Int. Geoscience Remote Sensing Congr.*, Munich, Germany, 2012, pp. 1251–1253.
- [37] J. Geng, H. Wang, J. Fan, and X. Ma, "SAR image classification via deep recurrent encoding neural networks," *IEEE T. Geosci. Remote Sens.*, vol. 56, no. 4, pp. 2255–2269, Apr. 2018.
- [38] X. Lu, B. Wang, X. Zheng, and X. Li, "Exploring models and data for remote sensing image caption generation," *IEEE T. Geosci. Remote Sens.*, vol. 56, no. 4, pp. 2183–2195, Apr. 2018.
- [39] H. Lyu, H. Lu, and L. Mou, "Learning a transferable change rule from a recurrent neural network for land cover change detection," *Remote Sens.*, vol. 8, no. 6, Jun. 2016, art. no. 506.
- [40] B. Qu, X. Li, D. Tao, and X. Lu, "Deep semantic understanding of high resolution remote sensing image," in *Int. Conf. Computer, Information and Telecommunication Systems*. Kunming, China: IEEE, 2016.
- [41] W. Byeon and T. M. Breuel, "Supervised texture segmentation using 2D LSTM networks," in *IEEE Int. Conf. Image Processing*, Paris, France, 2014, pp. 4373–4377.
- [42] J. P. H. N. Jaipuria, G. Habibi, "A transferable pedestrian motion prediction model for intersections with different geometries," 2018, [Online]. Available: arXiv:1806.09444.
- [43] L. Ballan, F. Castaldo, A. Alahi, F. Palmieri, and S. Savarese, "Knowledge transfer for scene-specific motion prediction," in *Proc. European Conference Computer Vision*, B. Leibe, J. Matas, N. Sebe, and M. Welling, Eds. Amsterdam, The Netherlands: Springer International Publishing, 2016, vol. 1, pp. 697–713.
- [44] M. Monfort, A. Liu, and B. D. Ziebart, "Intent prediction and trajectory forecasting via predictive inverse linear-quadratic regulation," in *AAAI Conf. Artificial Intelligence*, 2015, pp. 3672–3678.
- [45] H. Yu, Z. Wu, S. Wang, Y. Wang, and X. Ma, "Spatiotemporal recurrent convolutional networks for traffic prediction in transportation networks," *Sensors*, vol. 17, no. 7, 2017, art. no. 1501.
- [46] X. Ma, Z. Dai, Z. He, J. Ma, Y. Wang, and Y. Wang, "Learning traffic as images: A deep convolutional neural network for large-scale transportation network speed prediction," *Sensors*, vol. 17, no. 4, 2017, art. no. 818.
- [47] J. Zhang, Y. Zheng, and D. Qi, "Deep spatio-temporal residual networks for citywide crowd flows prediction," in *Proc. Thirty-First AAAI Conf. on Artificial Intelligence*, 2017, pp. 1655–1661.
- [48] J. Zhang, Y. Zheng, D. Qi, R. Li, and X. Yi, "DNN-based prediction model for spatio-temporal data," in *Proc. 24th ACM SIGSPATIAL Int. Conf. on Advances in Geographic Information Systems*, 2016, art. no. 92.
- [49] Y. Wu and H. Tan, "Short-term traffic flow forecasting with spatial-temporal correlation in a hybrid deep learning framework," 2016, [Online]. Available: arXiv:1612.01022.
- [50] J. Walker, C. Doersch, A. Gupta, and M. Hebert, "An uncertain future: Forecasting from static images using variational autoencoders," in *Proc. European Conference Computer Vision*, B. Leibe, J. Matas, N. Sebe, and M. Welling, Eds. Amsterdam, The Netherlands: Springer International Publishing, 2016, vol. 7, pp. 835–851.
- [51] J. Walker, A. Gupta, and M. Hebert, "Dense optical flow prediction from a static image," in *IEEE Int. Conf. Computer Vision*, Santiago, Chile, 2015, pp. 2443–2451.
- [52] S. L. Pinteá, J. C. V. Gemert, and A. W. M. Smeulders, "Déjà Vu: Motion prediction in static images," in *Proc. European Conference Computer*

- Vision, D. Fleet, T. Pajdla, B. Schiele, and T. Tuytelaars, Eds., vol. 3. Zurich, Switzerland: Springer, 2014, pp. 172–187.
- [53] A. X. Lee, R. Zhang, F. Ebert, P. Abbeel, C. Finn, and S. Levine, “Stochastic adversarial video prediction,” 2018, [Online]. Available: arXiv:1804.01523.
- [54] M. Babaeizadeh, C. Finn, D. Erhan, R. H. Campbell, and S. Levine, “Stochastic variational video prediction,” in *Int. Conf. Learning Representations*, 2018.
- [55] W. Lotter, G. Kreiman, and D. Cox, “Deep predictive coding networks for video prediction and unsupervised learning,” in *Int. Conf. Learning Representations*, Toulon, France, 2017.
- [56] R. Villegas, J. Yang, S. Hong, X. Lin, and H. Lee, “Decomposing motion and content for natural video sequence prediction,” in *Int. Conf. Learning Representations*, Toulon, France, 2017.
- [57] M. Mathieu, C. Couprie, and Y. Lecun, “Deep multi-scale video prediction beyond mean square error,” in *Int. Conf. Learning Representations*, San Juan, Puerto Rico, 2016.
- [58] V. Patraucean, A. Handa, and R. Cipolla, “Spatio-temporal video auto-encoder with differentiable memory,” in *Int. Conf. Learning Representations*, San Juan, Puerto Rico, 2016.
- [59] N. Srivastava, E. Mansimov, and R. Salakhudinov, “Unsupervised learning of video representations using LSTMs,” in *Proc. 32nd Int. Conf. Machine Learning*, 2015, pp. 843–852.
- [60] M. Ranzato, A. Szlam, J. Bruna, M. Mathieu, R. Collobert, and S. Chopra, “Video (language) modeling: a baseline for generative models of natural videos,” 2014, [Online]. Available: arXiv:1412.6604.
- [61] V. Michalski, R. Memisevic, and K. Konda, “Modeling deep temporal dependencies with recurrent “grammar cells,”” in *Advances Neural Information Processing Systems 27*, Z. Ghahramani, M. Welling, C. Cortes, N. D. Lawrence, and K. Q. Weinberger, Eds. Curran Associates, Inc., 2014, pp. 1925–1933.
- [62] D. J. Cavalieri, T. Markus, and J. C. Comiso, “AMSR-E/Aqua Daily L3 12.5 km Brightness Temperature, Sea Ice Concentration, & Snow Depth Polar Grids, Version 3,” Boulder, Colorado USA. NASA National Snow and Ice Data Center Distributed Active Archive Center. doi: [http://dx.doi.org/10.5067/AMSR-E/AE\\_SII2.003](http://dx.doi.org/10.5067/AMSR-E/AE_SII2.003). Accessed: Mar. 4, 2019., 2014.
- [63] JAXA, “Globe Portal System,” <https://gportal.jaxa.jp/gpr/index/index>. Accessed: Mar. 4, 2019., 2017.
- [64] Brigham Young University, “ASCAT Enhanced Resolution Image Products (beta version),” [http://www.scp.byu.edu/data/Ascat/SIR/Ascat\\_sir.html](http://www.scp.byu.edu/data/Ascat/SIR/Ascat_sir.html). Accessed: Mar. 4, 2019., 2018.
- [65] NSIDC, “Documentation: Polar stereographic projection and grid,” National Snow and Ice Data Center. [Online]. Available: [http://nsidc.org/data/polar-stereo/ps\\_grids.html](http://nsidc.org/data/polar-stereo/ps_grids.html). Accessed on: Mar. 4, 2019., 2016.
- [66] Z. I. Petrou, Y. Xian, and Y. Tian, “Towards breaking the spatial resolution barriers: An optical flow and super-resolution approach for sea ice motion estimation,” *ISPRS J. Photogramm.*, vol. 138, pp. 164–175, Apr. 2018.
- [67] Z. I. Petrou and Y. Tian, “High-resolution sea ice motion estimation with optical flow using satellite spectroradiometer data,” *IEEE T. Geosci. Remote Sens.*, vol. 55, no. 3, pp. 1339–1350, 2017.
- [68] J. K. Hutchings, P. Heil, A. Steer, and W. D. Hibler, “Subsynoptic scale spatial variability of sea ice deformation in the western Weddell Sea during early summer,” *J. Geophys. Res. Oceans*, vol. 117, no. C01002, Jan. 2012.
- [69] J. K. Hutchings, A. Roberts, C. A. Geiger, and J. Richter-Menge, “Spatial and temporal characterization of sea-ice deformation,” *Ann. Glaciol.*, vol. 52, no. 57, pp. 360–368, 2011.
- [70] T. Tieleman and G. Hinton, “Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude,” Coursera: Neural Networks for Machine Learning, 4, 26–31, 2012.
- [71] R. Jozefowicz, W. Zaremba, and I. Sutskever, “An empirical exploration of recurrent network architectures,” in *Proc. 32nd Int. Conf. on Machine Learning*, ser. ICML’15, vol. 37, 2015, pp. 2342–2350.
- [72] W. N. Meier and M. Dai, “High-resolution sea-ice motions from AMSR-E imagery,” *Ann. Glaciol.*, vol. 44, pp. 352–356, Nov. 2006.
- [73] T. Lavergne, S. Eastwood, Z. Teffah, H. Schyberg, and L. A. Breivik, “Sea ice motion from low-resolution satellite sensors: An alternative method and its validation in the Arctic,” *J. Geophys. Res.*, vol. 115, Oct. 2010.
- [74] M. Tschudi, C. Fowler, J. Maslanik, J. S. Stewart, and W. Meier, “Polar Pathfinder daily 25 km EASE-Grid sea ice motion vectors, version 3, Buoy,” Boulder, Colorado USA: National Snow and Ice Data Center. doi: <http://dx.doi.org/10.5067/O57VAIT2AYYY>. Accessed: Mar. 4, 2019., 2016.



**Zisis I. Petrou** (S’05–M’15) received the Diploma in electrical and computer engineering from the Aristotle University of Thessaloniki, Greece, in 2007 and the M.Sc. degree in space studies from the International Space University, Strasbourg, France, in 2009. In 2015, he received the Ph.D. degree in remote sensing from the Department of Electrical and Electronic Engineering, Imperial College London, United Kingdom.

From 2009 to 2016, he was a Research Assistant with the Centre for Research and Technology Hellas, Thessaloniki, Greece. From 2016 to 2017, he was a Postdoctoral Research Scholar with the City College of New York, City University of New York. He currently works as data scientist and machine learning engineer in tech. His research interests include classification, motion detection and prediction analysis on remote sensing images using advanced machine learning, image processing, and computer vision techniques.

Dr. Petrou was the recipient of the Best Paper Award for Young Professionals under 35 at the 2nd International Conference on Space Technology, Athens, in 2011, sponsored by IEEE. He has been a scholar of the European Space Agency (ESA) and the Onassis Foundation, Greece.



**Yingli Tian** (M’99–SM’01–F’18) received the B.S. and M.S. degrees from Tianjin University, China, in 1987 and 1990, and the Ph.D. degree from Chinese University of Hong Kong, Hong Kong, in 1996.

After holding a faculty position at National Laboratory of Pattern Recognition, Chinese Academy of Sciences, Beijing, she joined Carnegie Mellon University in 1998, where she was a postdoctoral fellow at the Robotics Institute. She then worked as a research staff member in IBM T. J. Watson Research Center from 2001 to 2008. She is one of

the inventors of the IBM Smart Surveillance Solutions. She is a professor in the Department of Electrical Engineering at the City College and the department of Computer Science at the Graduate Center, City University of New York since 2008. Her current research focuses on remote sensing and a wide range of computer vision problems from object recognition, scene understanding, to human behavior analysis, facial expression recognition, and assistive technology. She is a fellow of IEEE.